# Using Space Effectively: 2D 

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CS 294-10: Visualization
Fall 2008

## Assignment 3: Visualization Software

Create an interactive visualization application - you choose data domain and visualization technique.

1. Describe data and storyboard interface due Oct 1 (before class)
2. Implement interface and produce final writeup due Oct 13 (before class)
3. Submit the application and a final writeup on the wiki


Can work alone or in pairs
Final write up due before class on Oct 13, 2008

## Topics

Displaying data in graphs
Banking to 45 degrees
Fitting data and depicting residuals
Displaying multidimensional data
Graphical calculations
Zooming and distortion


## Effective use of space

Which graph is better?


Government payrolls in 1937 [How To Lie With Statistics. Huff 93]

## Aspect ratio

Fill space with data
Don't worry about showing zero


Yearly CO2 concentrations [Cleveland 85]

## Clearly mark scale breaks



## Scale break vs. Log scale


[Cleveland 85]

## Scale break vs. Log scale


[Cleveland 85]
Both increase visual resolution

- Log scale - easy comparisons of all data
- Scale break - more difficult to compare across break


## Linear scale vs. Log scale




## Linear scale vs. Log scale

Linear scale

- Absolute change


Log scale

- Small fluctuations
- Percent change $d(10,20)=d(30,60)$



## Semilog graph: Exponential growth

Exponential functions $\left(\mathrm{y}=\mathrm{ka}^{\mathrm{mx}}\right.$ ) transform into lines
$\log (\mathrm{y})=\log (\mathrm{k})+\log (\mathrm{a}) \mathrm{mx}$
Intercept: $\log (\mathrm{k})$
Slope: $\quad \log (a) m$


$y=6^{0.5 x}$, slope in semilog space: $\log (6)^{*} 0.5=0.3891$

## Semilog graph: Exponential decay

Exponential functions $\left(\mathrm{y}=\mathrm{ka}^{\mathrm{mx}}\right.$ ) transform into lines $\log (\mathrm{y})=\log (\mathrm{k})+\log (\mathrm{a}) \mathrm{mx}$ Intercept: $\log (\mathrm{k})$
Slope: $\quad \log (a) m$

$y=0.5^{2 x}$, slope in semilog space: $\log (0.7) * 2=-0.3098$

## Semilog graph: Lines

Exponential functions $\left(\mathrm{y}=\mathrm{ka}^{\mathrm{mx}}\right.$ ) transform into lines
$\log (\mathrm{y})=\log (\mathrm{k})+\log (\mathrm{a}) \mathrm{mx}$ Intercept: $\log (\mathrm{k})$
Slope: $\quad \log (a) m$


$\mathrm{y}=\mathrm{x}$, slope in semilog gives instantaneous : $\log (\mathbf{a}) \mathrm{m}$

## Semilog graph

Exponential functions $\left(\mathrm{y}=\mathrm{ka}^{\mathrm{mx}}\right.$ ) transform into lines $\log (\mathrm{y})=\log (\mathrm{k})+\log (\mathrm{a}) \mathrm{m} \mathrm{x}$


SARS cases up March - July 7, 2003 http://www.squeak.org/us/ted/sars-graph.html

AIDS Cases: http://www.righto.com/java/statsgraph.html

## Log-Log graph

Power functions ( $\mathrm{y}=\mathrm{kx}^{\mathrm{a}}$ ) transform into lines
Example - Steven's power laws:

$$
S=k l^{p} \rightarrow \log S=\log k+p \log I
$$




## Banking to 45 Degrees

## Aspect ratio

Fill space with data
Don't worry about showing zero



Yearly CO2 concentrations [Cleveland 85]


## Banking to 45 degrees





Two segments are maximally discriminable when avg absolute angle is $45^{\circ}$

Optimize the aspect ratio by banking to $45^{\circ}$

## Aspect-ratio banking techniques

Median-Absolute-Slope

$$
\alpha=\operatorname{median}\left|s_{i}\right| R_{x} / R_{y}
$$

Average-Absolute-Orientation Unweighted

$$
\sum_{i} \frac{\left|\theta_{i}(\alpha)\right|}{n}=45^{\circ}
$$

Weighted

$$
\frac{\sum_{i}\left|\theta_{i}(\alpha)\right| l_{i}(\alpha)}{\sum_{i} l_{i}(\alpha)}=45^{\circ}
$$

Average-Absolute-Slope

$$
\alpha=\operatorname{mean}\left|s_{i}\right| R_{x} / R_{y}
$$

Max-Orientation-Resolution Global (over all i, j s.t. i: $\neq \mathrm{j}$ )

$$
\sum_{i} \sum_{i}\left|\theta_{i}(\alpha)-\theta_{j}(\alpha)\right|^{2}
$$

Local (over adjacent segments)

$$
\sum_{i}\left|\theta_{i}(\alpha)-\theta_{i+1}(\alpha)\right|^{2}
$$

## Slopeless line culling



Standard, Aspect Ratio = 1.97
Culled, Aspect Ratio = 4.00

Exclude line segments with zero or infinite slope

## Comparison (Results)



## Discussion

Due to computational complexity...
Prefer avg-slope to avg-weighted-orient
Prefer avg-orient to global-orient-resolution
But due to perceptual effectiveness... ?
Cleveland recommends weighted-avg-orient But, goal is to maximize discriminability

Perceptual experiments needed to clarify


## Applications

Small Multiples Displays Trend Explorer


Sparklines
Banking can be applied to create sparklines, data-intense, word-sized graphics. A plot might be included inline womblumevilid, supporting uninterrupted reading

| VFINX |  | 119.27 |  |
| :--- | :--- | :--- | :--- |
| GOOG |  | 27.14 |  |
| MSFT |  |  |  |
| YHOO |  |  |  |



## Fitting the Data




## Transforming data

How well does curve fit data?

[Cleveland 85]

## Transforming data

Residual graph

- Plot vertical distance from best fit curve
- Residual graph shows accuracy of fit


[Cleveland 85]


## Most powerful brain?



The Dragons of Eden [Carl Sagan]


