

# Using Space Effectively: 2D

*Maneesh Agrawala*

CS 294-10: Visualization  
Fall 2007

## Assignment 3: Visualization Software

Create an interactive visualization application – you choose data domain and visualization technique.

1. Describe data and storyboard interface  
**due Oct 3 (before class)**
2. Implement interface and produce final writeup  
**due Oct 15 (before class)**
3. Submit the application and a final writeup on the wiki



Can work alone or in pairs  
Final write up due before class on **Oct 15, 2007**

## **Topics**

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**Rearrangements/Reorderable spaces**

**Displaying data in graphs**

**Banking to 45 degrees**

**Fitting data and depicting residuals**

**Displaying multidimensional data**

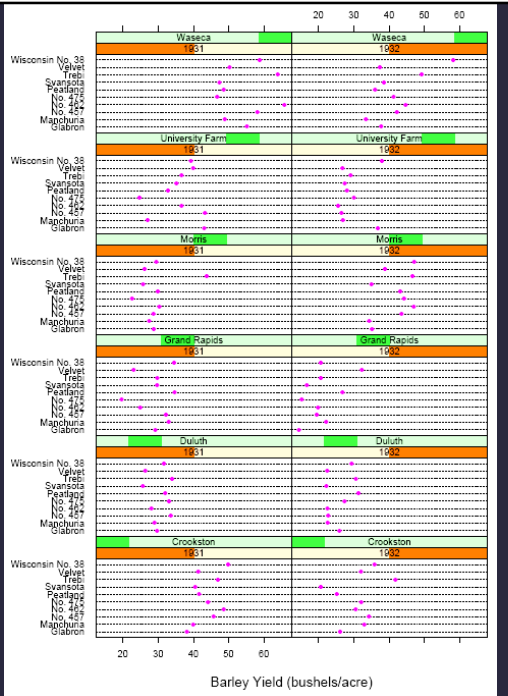
**Graphical calculations**

**Zooming and distortion**

## **Reorderable Spaces**

# Trellis

[Becker, Cleveland, and Shyu 96]



Condition variables

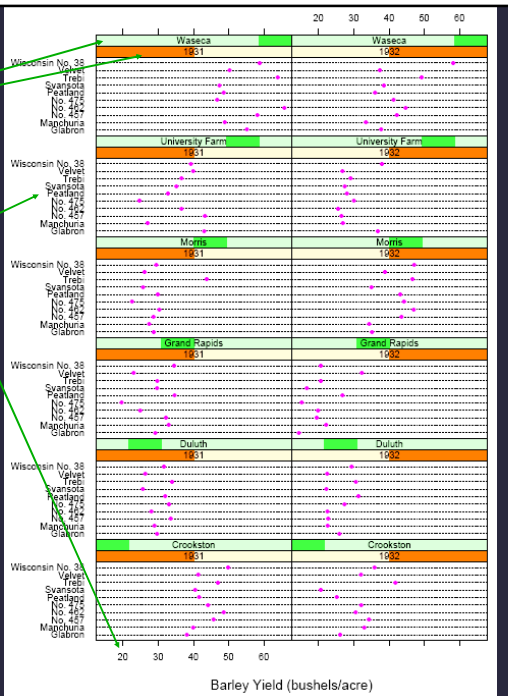
location, year

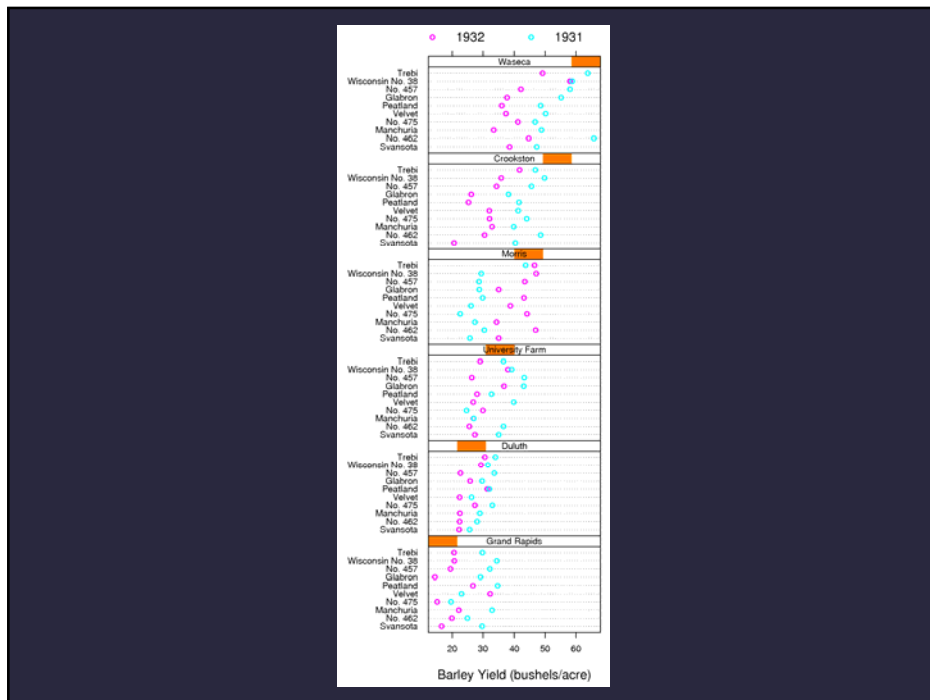
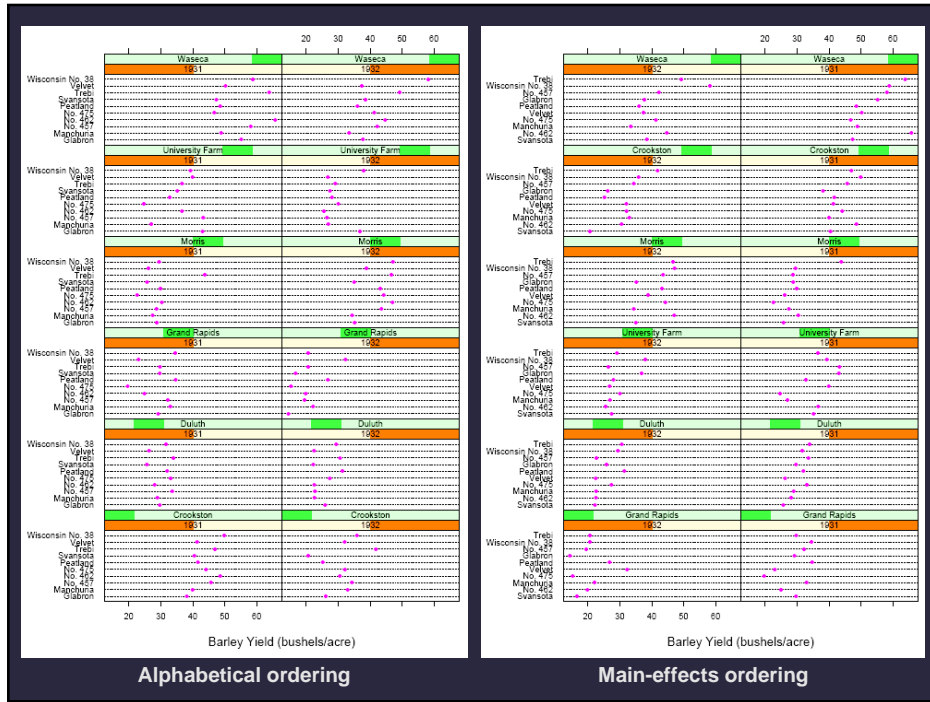
Panel variables

type, yield

# Trellis

[Becker, Cleveland, and Shyu 96]

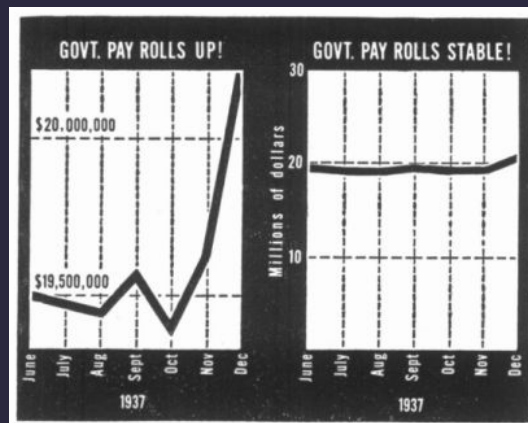




# Graphs and Lines

## Effective use of space

Which graph is better?

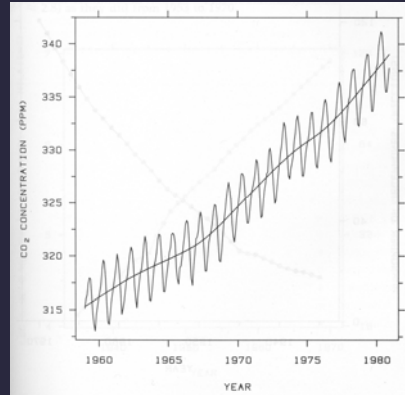
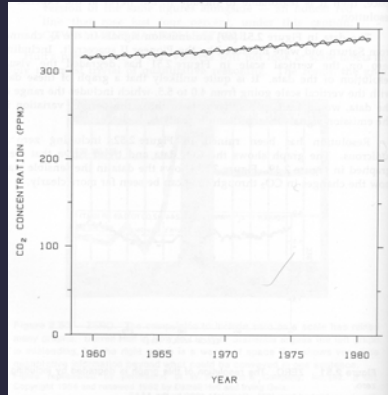


Government payrolls in 1937 [How To Lie With Statistics. Huff 93]

# Aspect ratio

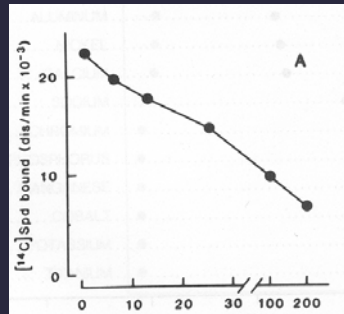
Fill space with data

Don't worry about showing zero

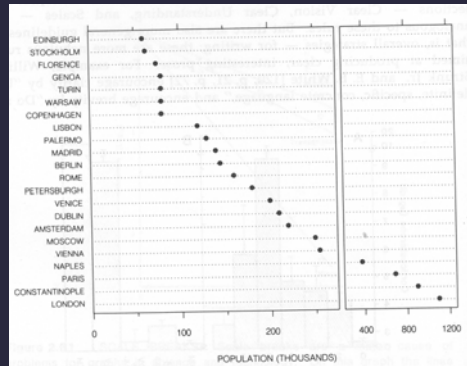


Yearly CO<sub>2</sub> concentrations [Cleveland 85]

# Clearly mark scale breaks

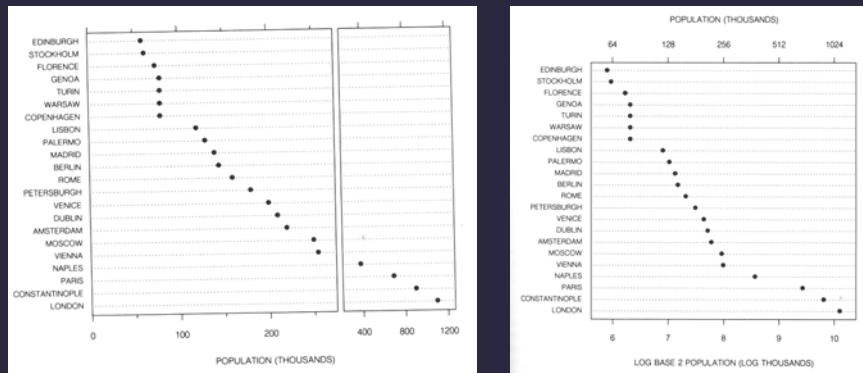


Poor scale break [Cleveland 85]



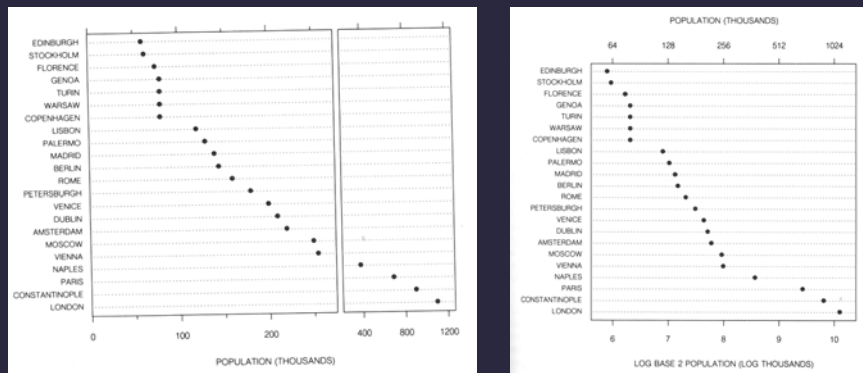
Well marked scale break [Cleveland 85]

# Scale break vs. Log scale



[Cleveland 85]

# Scale break vs. Log scale

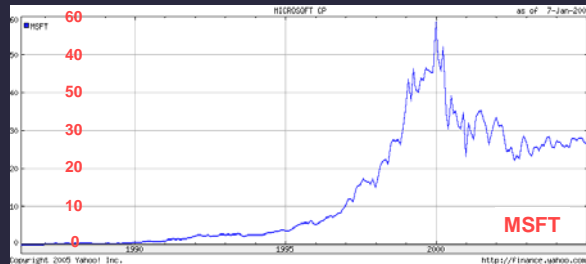


[Cleveland 85]

Both increase visual resolution

- Log scale - easy comparisons of all data
- Scale break – more difficult to compare across break

# Linear scale vs. Log scale



# Linear scale vs. Log scale

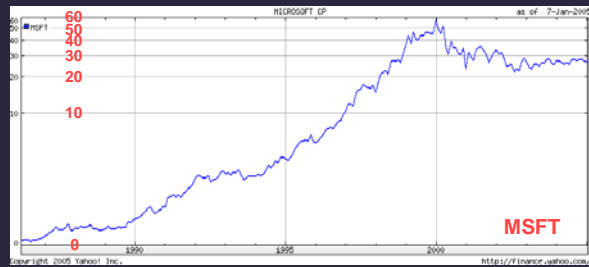
## Linear scale

- Absolute change



## Log scale

- Small fluctuations
  - Percent change
- $d(10,20) = d(30,60)$





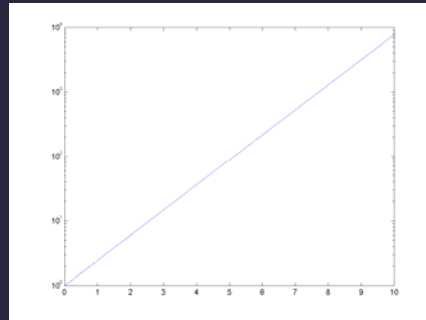
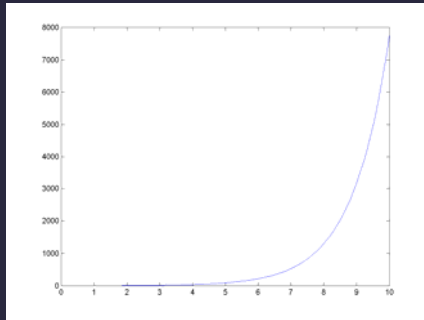
## Semilog graph: Exponential growth

Exponential functions ( $y = ka^{mx}$ ) transform into lines

$$\log(y) = \log(k) + \log(a)mx$$

Intercept:  $\log(k)$

Slope:  $\log(a)m$



$$y = 6^{0.5x}, \text{ slope in semilog space: } \log(6) * 0.5 = 0.3891$$

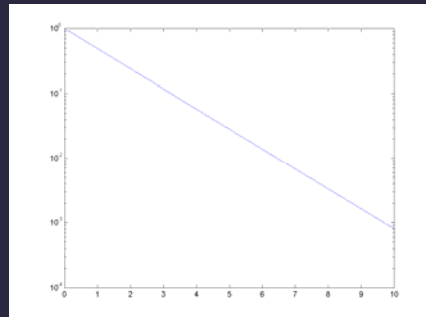
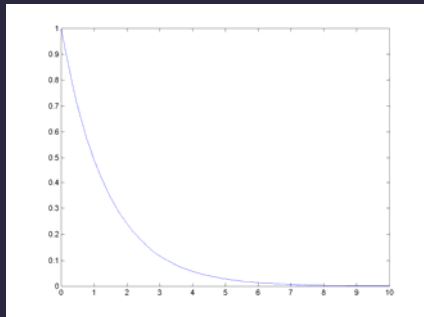
## Semilog graph: Exponential decay

Exponential functions ( $y = ka^{mx}$ ) transform into lines

$$\log(y) = \log(k) + \log(a)mx$$

Intercept:  $\log(k)$

Slope:  $\log(a)m$



$$y = 0.5^{2x}, \text{ slope in semilog space: } \log(0.7) * 2 = -0.3098$$

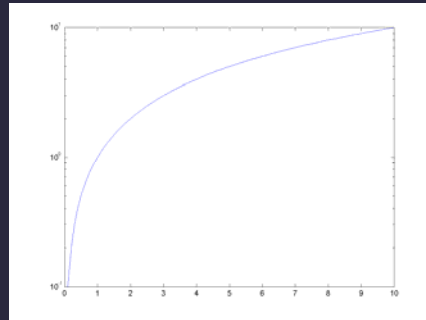
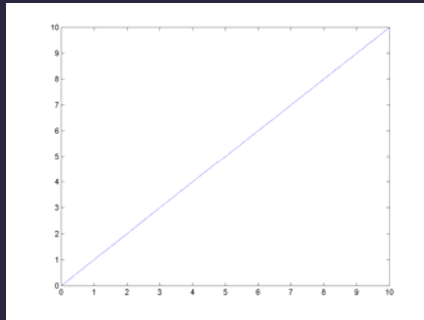
## Semilog graph: Lines

Exponential functions ( $y = ka^{mx}$ ) transform into lines

$$\log(y) = \log(k) + \log(a)mx$$

Intercept:  $\log(k)$

Slope:  $\log(a)m$

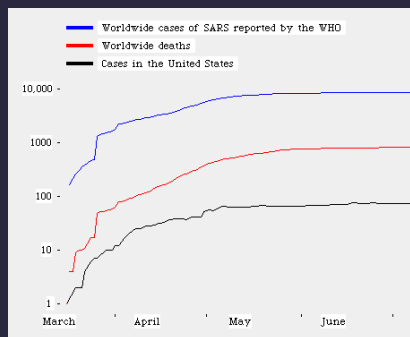


$y = x$  , slope in semilog gives instantaneous :  $\log(a)m$

## Semilog graph

Exponential functions ( $y = ka^{mx}$ ) transform into lines

$$\log(y) = \log(k) + \log(a)mx$$



SARS cases up March – July 7, 2003

<http://www.squeak.org/us/ted/sars-graph.html>

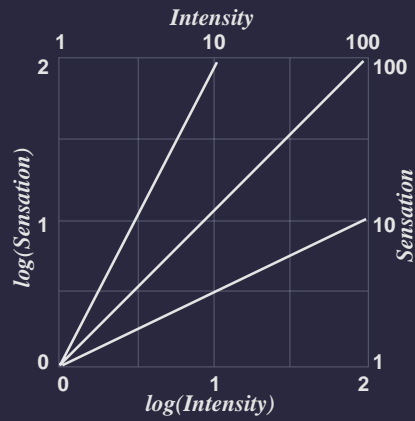
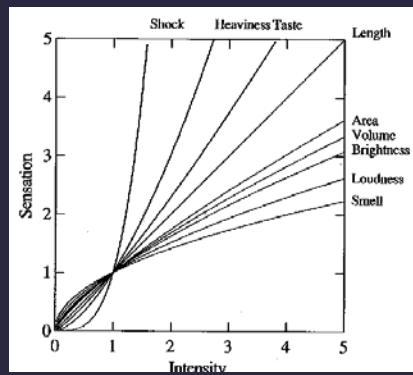
AIDS Cases: <http://www.righto.com/java/statsgraph.html>

## Log-Log graph

Power functions ( $y = kx^a$ ) transform into lines

Example - Steven's power laws:

$$S = kI^p \rightarrow \log S = \log k + p \log I$$

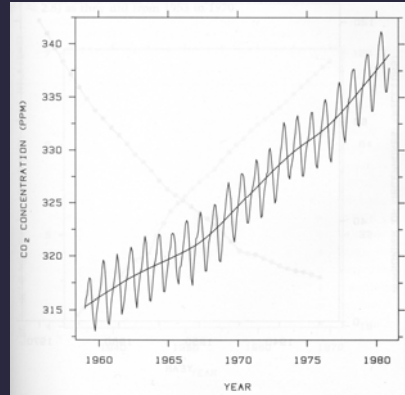
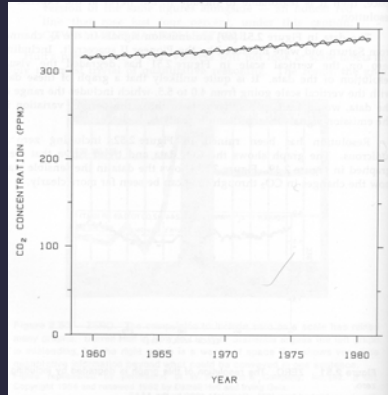


## Banking to 45 Degrees

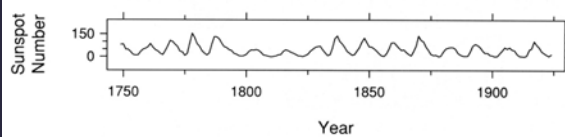
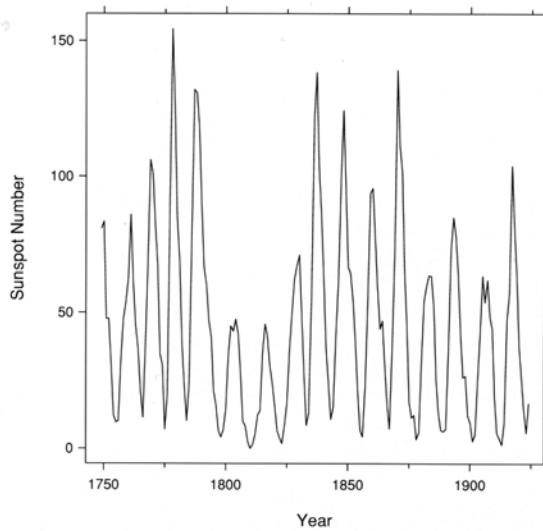
# Aspect ratio

Fill space with data

Don't worry about showing zero



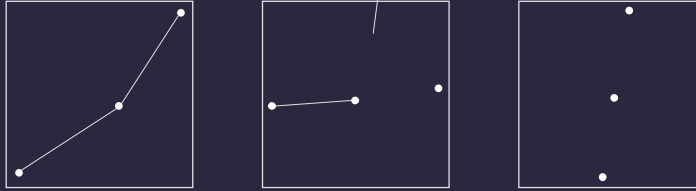
Yearly CO<sub>2</sub> concentrations [Cleveland 85]



William S. Cleveland  
*The Elements of  
Graphing Data*

## Banking to 45 degrees

To facilitate perception of trends, maximize the discriminability of line segment orientations



Two line segments are maximally discriminable when their average absolute angle is  $45^\circ$

Optimize the *aspect ratio* to bank to  $45^\circ$

## Aspect-ratio banking techniques

### Median-Absolute-Slope

$$\alpha = \text{median } |s_i| R_x / R_y$$

### Average-Absolute-Slope

$$\alpha = \text{mean } |s_i| R_x / R_y$$

### Average-Absolute-Orientation

Unweighted

$$\sum_i \frac{|\theta_i(\alpha)|}{n} = 45^\circ$$

### Max-Orientation-Resolution

Global (over all  $i, j$  s.t.  $i \neq j$ )

$$\sum_i \sum_j |\theta_i(\alpha) - \theta_j(\alpha)|^2$$

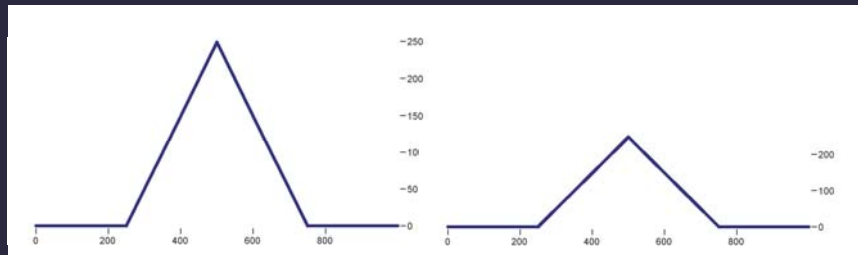
Weighted

$$\frac{\sum_i |\theta_i(\alpha)| l_i(\alpha)}{\sum_i l_i(\alpha)} = 45^\circ$$

Local (over adjacent segments)

$$\sum_i |\theta_i(\alpha) - \theta_{i+1}(\alpha)|^2$$

# Slopeless line culling

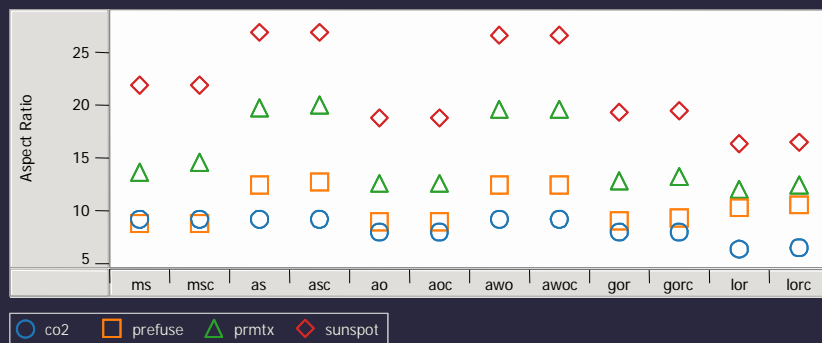


Standard, Aspect Ratio = 1.97

Culled, Aspect Ratio = 4.00

Exclude line segments with zero or infinite slope

# Comparison (Results)



## Discussion

Due to computational complexity...

Prefer avg-slope to avg-weighted-orient

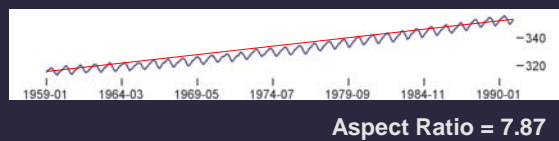
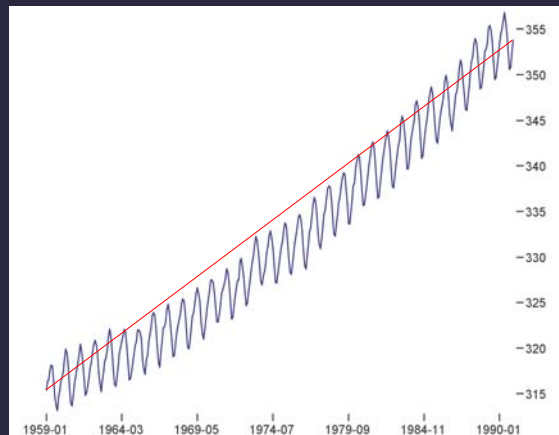
Prefer avg-orient to global-orient-resolution

But due to perceptual effectiveness... ?

Cleveland recommends weighted-avg-orient

But, goal is to maximize discriminability

Perceptual experiments needed to clarify



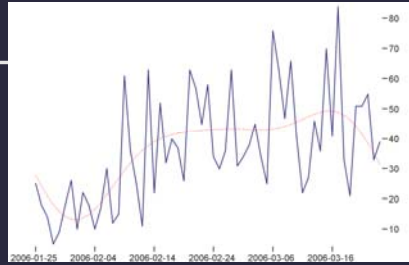
CO<sub>2</sub> Measurements

William S. Cleveland  
*Visualizing Data*

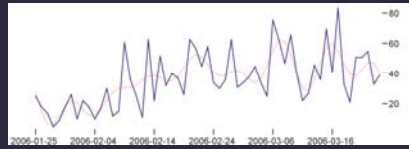
# Downloads

Two months of daily  
prefuse downloads

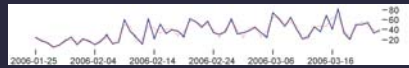
Aspect Ratio = 1.44



Aspect Ratio = 2.89



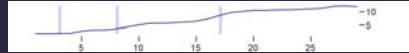
Aspect Ratio = 8.81



Power Spectrum

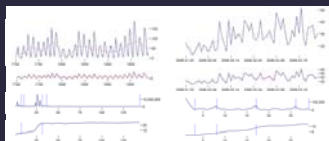


Aspect Ratios

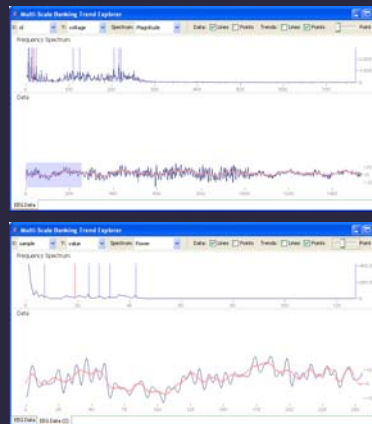


# Applications


Small Multiples Displays











Trend Explorer



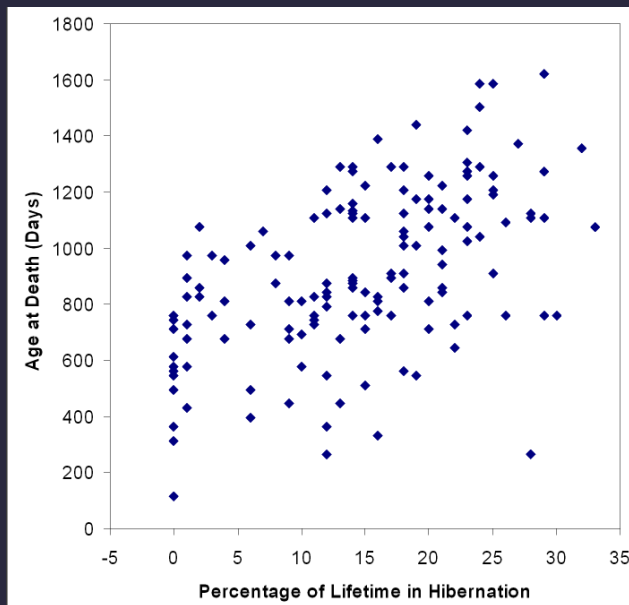
Sparklines

Banking can be applied to create *sparklines*, data-intense, word-sized graphics. A plot might be included inline , supporting uninterrupted reading.

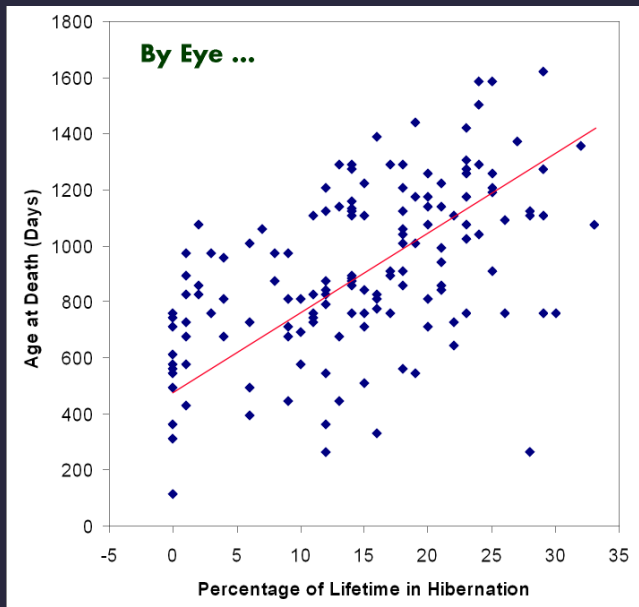
<b>VFINX</b>		<b>119.27</b>	
<b>GOOG</b>		<b>364.80</b>	
<b>MSFT</b>		<b>27.14</b>	
<b>YHOO</b>		<b>32.18</b>	



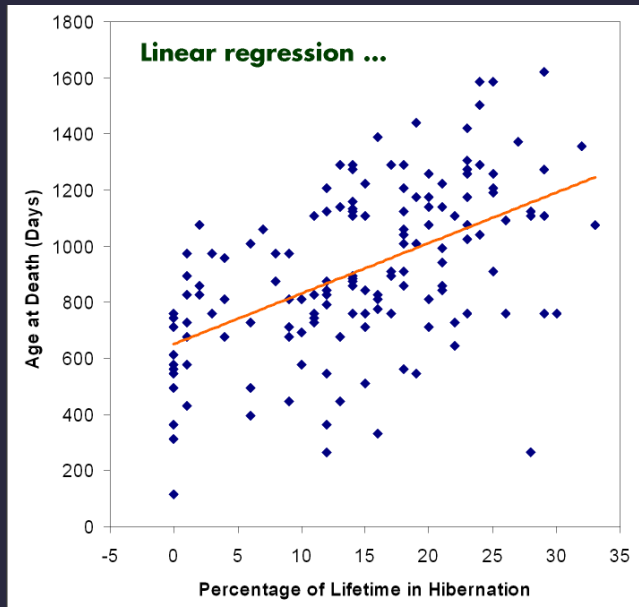
# Fitting the Data



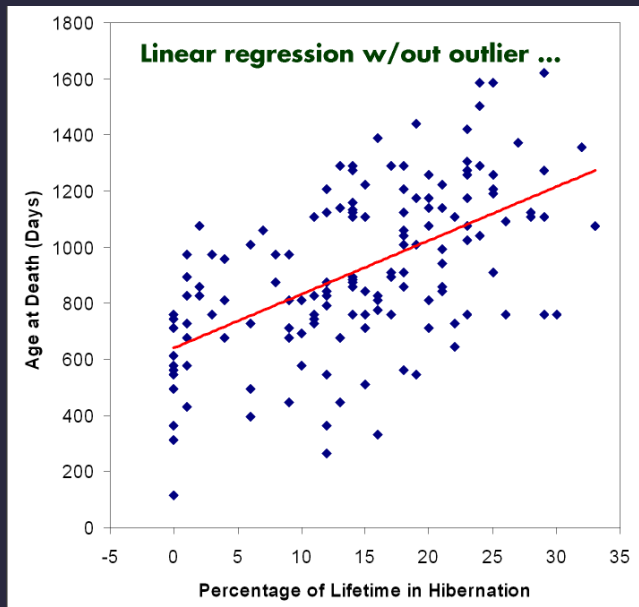
[The Elements of Graphing Data. Cleveland 94]



[The Elements of Graphing Data. Cleveland 94]



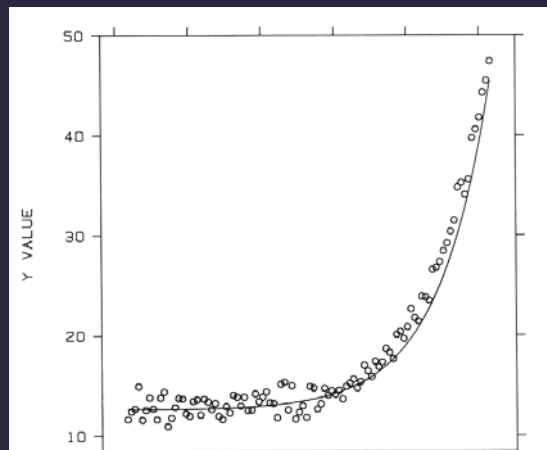
[The Elements of Graphing Data. Cleveland 94]



[The Elements of Graphing Data. Cleveland 94]

## Transforming data

How well does curve fit data?

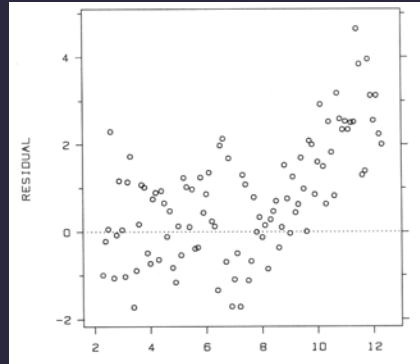
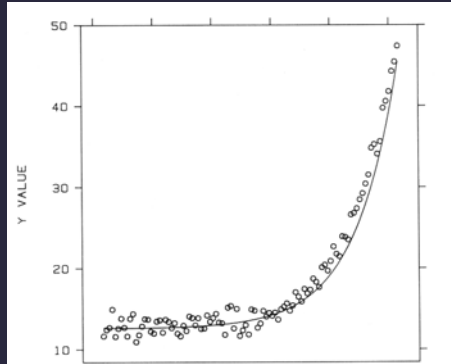


[Cleveland 85]

# Transforming data

## Residual graph

- Plot vertical distance from best fit curve
- Residual graph shows accuracy of fit

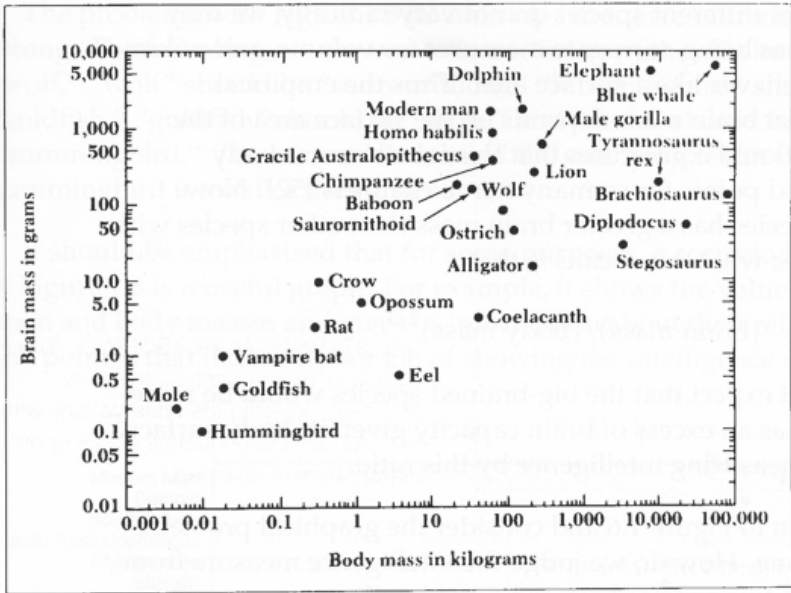


[Cleveland 85]

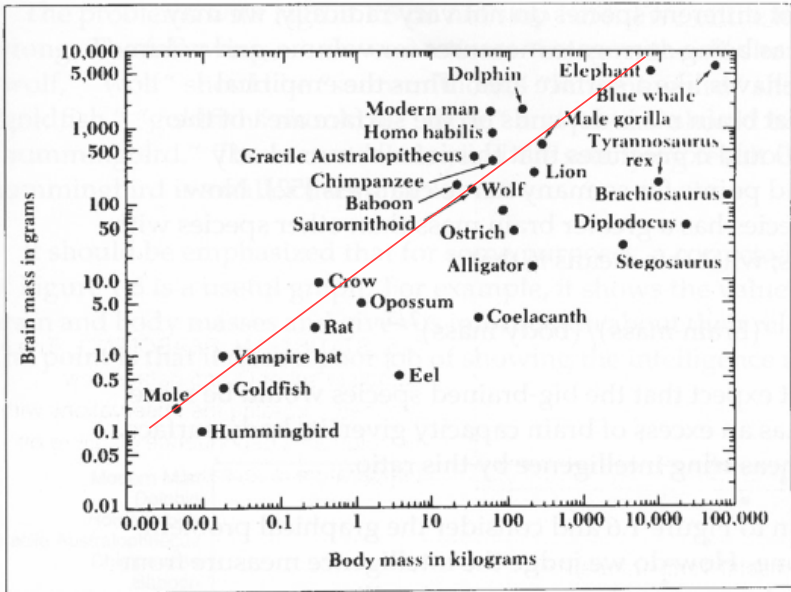
# Most powerful brain?

A screenshot of a Microsoft Excel spreadsheet titled 'animal.xls'. The spreadsheet contains a table with the following data:

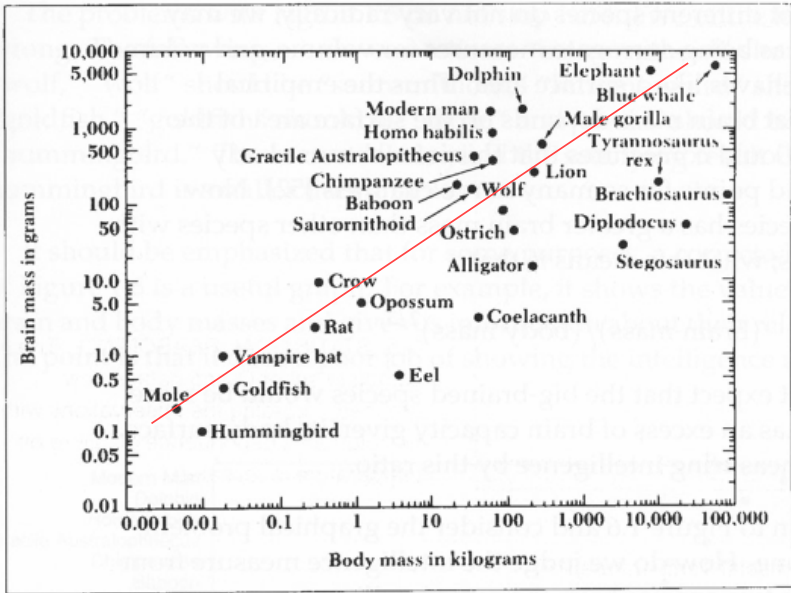
ID	Name	Body Weight	Brain Weight
1	1 Lesser Short-tailed Shrew	5	0.14
2	2 Little Brown Bat	10	0.25
3	3 Mouse	23	0.3
4	4 Big Brown Bat	23	0.4
5	5 Musk Shrew	48	0.33
6	6 Star Nosed Mole	60	1
7	7 Eastern American Mole	75	1.2
8	8 Ground Squirrel	101	4
9	9 Tree Shrew	104	2.5
10	10 Golden Hamster	120	1
11	11 Mole Rate	122	3
12	12 Galago	200	5
13	13 Rat	280	1.9
14	14 Chinchilla	425	6.4
15	15 Desert Hedgehog	550	2.4
16	16 Rock Hyrax (a)	750	12.3
17	17 European Hedgehog	785	3.5
18	18 Tenrec	900	2.6
19	19 Arctic Ground Squirrel	920	5.7
20	20 African Giant Pouched Rat	1000	6.6
21	21 Guinea Pig	1040	5.5
22	22 Mountain Beaver	1350	8.1
23	23 Slow Loris	1400	12.5
24	24 Genet	1410	17.5
25	25 Phalanger	1620	11.4



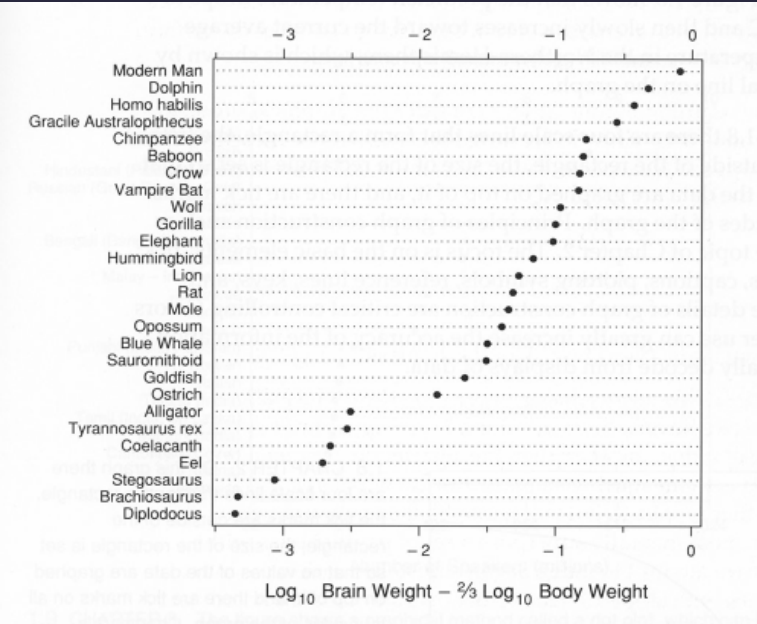
The Dragons of Eden [Carl Sagan]



The Dragons of Eden [Carl Sagan]



The Dragons of Eden [Carl Sagan]



The Elements of Graphing Data [Cleveland]

# Parallel Coordinates

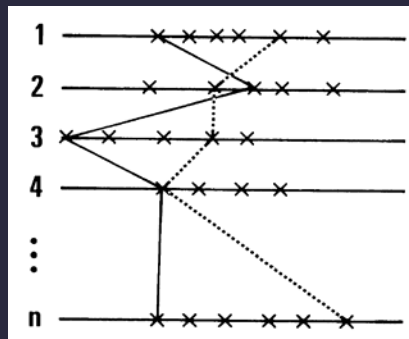
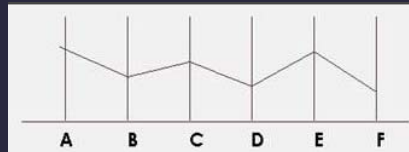
## Parallel coordinates

Visualizing nD in planar image

- Only 2 orthogonal axes
- Use parallel axes instead

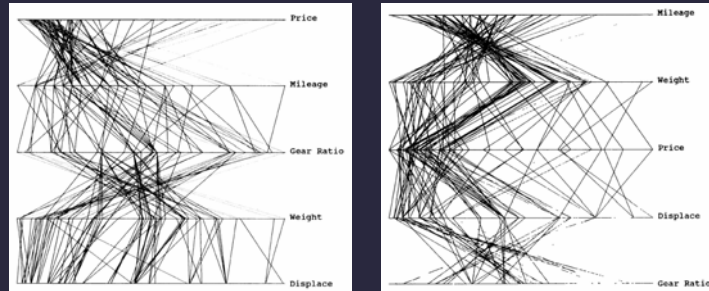
Plot each dimension of point  $x$  on separate axis

- $x = (a, b, c, d, \dots)$



[Wegman 90]

# Parallel coordinates: Axis ordering

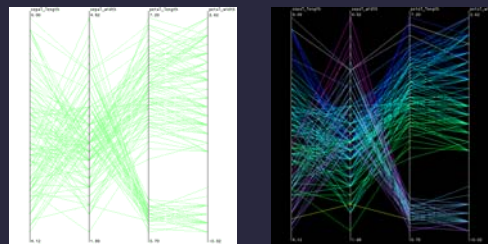


5D Automobile Data [Wegman 90]

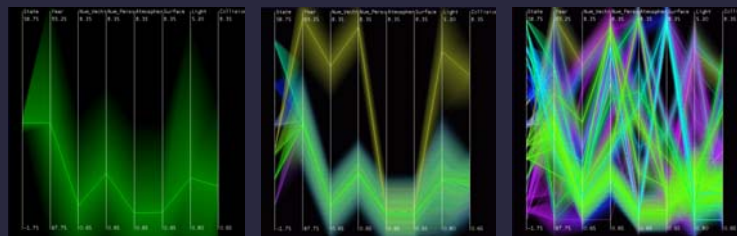
## No intrinsic axis order

- Interactive axis swap
  - Bad: Relies on human examination
  - Good: Powerful interaction
- Machine learning of axis order [Inselberg 99]

# Parallel coordinates



Proximity-based coloring



Visualizing hierarchical clusters

[Fua et al. 99]